

HW #22

Solutions EE301

Ch. 16 #s 10, 12ab, 15

$$16.10) \quad e_1 = 10V \sin(\omega t + 30^\circ)$$

$$e_2 = 15V \sin(\omega t - 20^\circ)$$

$$v = e_1 + e_2$$

a. Convert e_1 and e_2 to phasor form

$$E_1 = 10V \angle 30^\circ$$

$$E_2 = 15V \angle -20^\circ$$

b. Determine $V = E_1 + E_2$

$$V = 10V \angle 30^\circ + 15V \angle -20^\circ$$

$$= (10V \cos 30^\circ + 10V \sin 30^\circ j) + (15V \cos(-20^\circ) + 15V \sin(-20^\circ)j)$$

$$= 8.66V + 5.0Vj + 14.10V - 5.13Vj$$

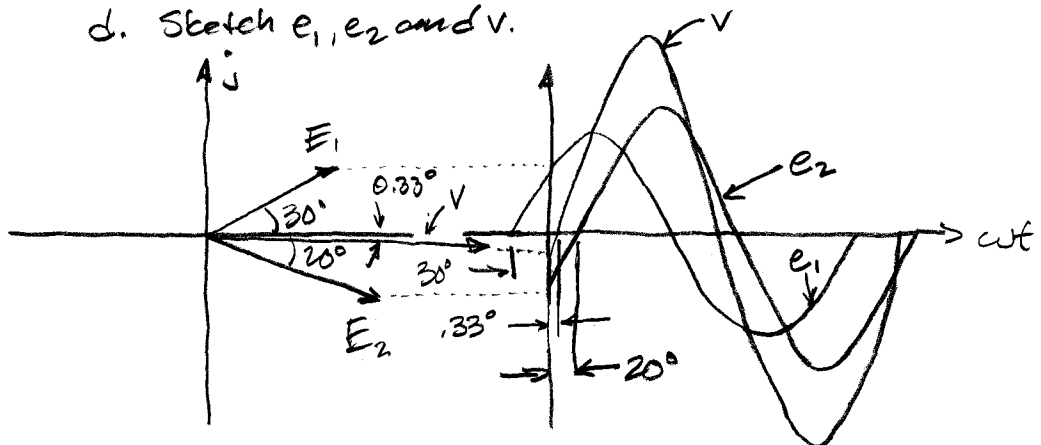
$$= 22.76V - 0.13Vj$$

$$= \sqrt{(22.76V)^2 + (0.13V)^2} \angle \tan^{-1}\left(\frac{-0.13V}{22.76V}\right)$$

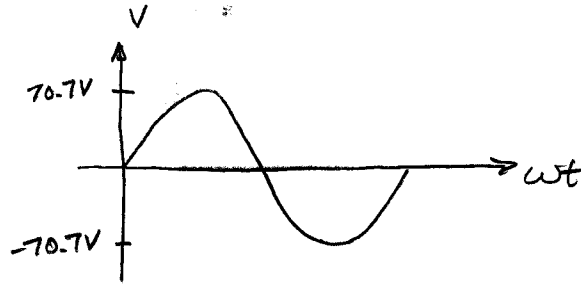
$$V = 22.8V \angle -0.33^\circ$$

c. Convert V to time domain

$$V = 22.8V \sin(\omega t - 0.33^\circ)$$

d. Sketch e_1 , e_2 and v .

16.12) a.



Express as time domain and phasor domain

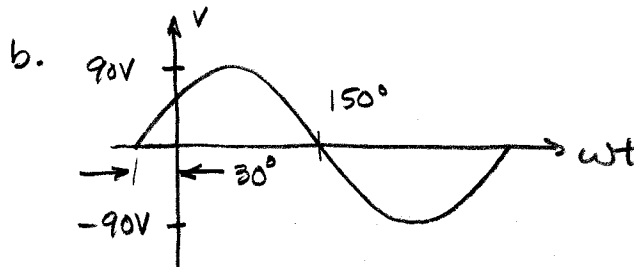
$$v = 70.7V \sin \omega t$$

$$V = V_{RMS} \angle 0^\circ$$

$$V = (0.707)(70.7V) \angle 0^\circ$$

$$V = 50V \angle 0^\circ$$

Note: From now on, we will use RMS (Effective) values for phasor voltages and currents.



$$v = 90V \sin(\omega t + 30^\circ)$$

$$V = V_{RMS} \angle 30^\circ = (0.707)(90V) \angle 30^\circ$$

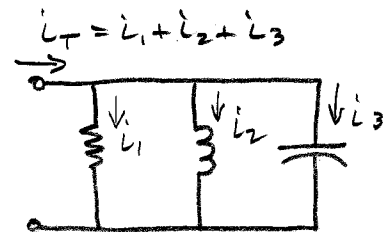
$$V = 63.6V \angle 30^\circ$$

16.15)

$$i_1 = 7mA \sin \omega t$$

$$i_2 = 4mA \sin(\omega t - 90^\circ)$$

$$i_3 = 6mA \sin(\omega t + 90^\circ)$$



a. Phasors

$$I_1 = (0.707)(7mA) \angle 0^\circ = 4.95mA \angle 0^\circ$$

$$I_2 = (0.707)(4mA) \angle -90^\circ = 2.83mA \angle -90^\circ$$

$$I_3 = (0.707)(6mA) \angle 90^\circ = 4.24mA \angle 90^\circ$$

$$I_T = 4.95mA \angle 0^\circ + 2.83mA \angle -90^\circ + 4.24mA \angle 90^\circ$$

$$= (4.95mA + 0j) + 2.83mA \cos(90^\circ) + 2.83mA \sin(-90^\circ)j + 4.24mA \cos(90^\circ) + 4.24mA \sin(90^\circ)j$$

$$= 4.95mA - 2.83mA j + 4.24mA j$$

$$= 4.95mA + 1.41mA j$$

$$I_T = \sqrt{(4.95mA)^2 + (1.41mA)^2} \angle \tan^{-1}\left(\frac{1.41}{4.95}\right) = 5.1mA \angle 15.9^\circ$$

b. time domain, i_T

$$i_T = \frac{5.1mA}{0.707} \sin(\omega t + 15.9^\circ)$$

$$i_T = 7.2mA \sin(\omega t + 15.9^\circ)$$