

LO-19

$$a) \quad \tau = R_{TH} C$$

$$R_{TH} = 100\text{ k}\Omega$$

$$C = 5.6\text{ nF}$$

$$\tau = 100000 \cdot 5.6 \times 10^{-9} \text{ F}$$

$$= 0.56\text{ s} = 560\text{ ms}$$

$$b) \quad V_C = V_f + (V_i - V_f) e^{-t/\tau}$$

$$V_f = 20\text{ V}$$

$V_i = 0\text{ V}$ Assuming capacitor fully discharged prior to shutting switch.

$$\Rightarrow V_C(t) = 20\text{ V} - 20\text{ V} e^{-t/560\text{ ms}}$$

$$c) \quad V_C(1\tau) = 20\text{ V} - 20\text{ V} e^{-1/560\text{ ms}}$$

$$V_C(1\tau) = 12.6\text{ V}$$

$$V_C(3\tau) = 20\text{ V} - 20\text{ V} e^{-3/560\text{ ms}}$$

$$V_C(3\tau) = 19.0\text{ V}$$

$$V_C(5\tau) = 20\text{ V} - 20\text{ V} e^{-5/560\text{ ms}}$$

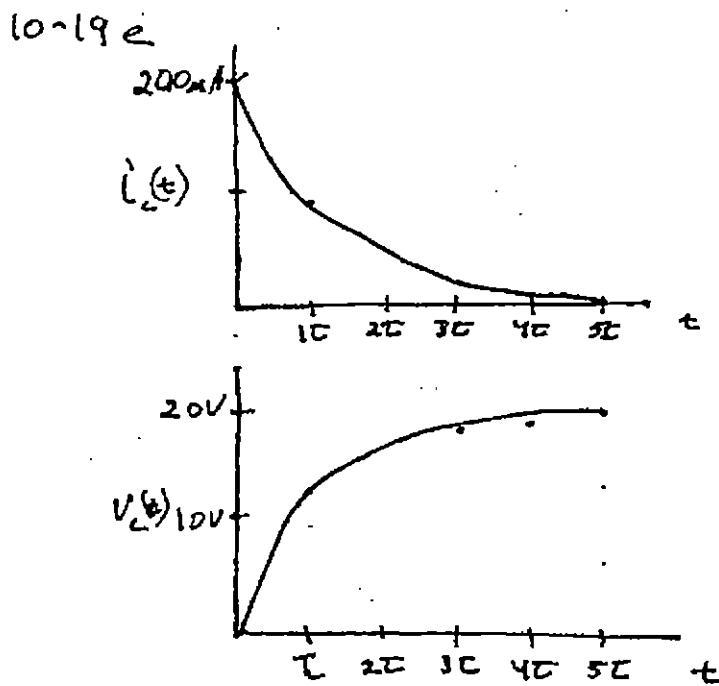
$$V_C(5\tau) = 19.9\text{ V}$$

$$d) \quad i_C = \frac{E - V_C}{R} = \frac{20 - (20 - 20e^{-t/560\text{ ms}})}{100\text{ k}\Omega}$$

$$= \frac{20\text{ V}}{100 \cdot 10^3 \text{ }\Omega} e^{-t/560\text{ ms}}$$

$$i_C = 200\text{ mA} e^{-t/560\text{ ms}}$$

$$\text{KVL: } V_f = E - V_C = 20\text{ V} e^{-t/560\text{ ms}} = V_f$$



10-25.

a. $T = R_{TH}C = 4.7k\Omega \cdot 56\mu F = 263.2ms$

b. $V_c(t) = V_f + (V_i - V_f)e^{-t/T}$

$$V_f = 22V$$

$V_i = 0V$ Assuming CAP is fully discharged to start.

Post. 1
$$V_c(t) = 22V \left(1 - e^{-t/263.2ms}\right) \quad 0 < t \leq 1s$$

$$i_c(t) = \frac{V_c(t)}{R}$$

KVL: $V_r(t) = E - V_c(t) \Rightarrow i_c(t) = \frac{E - V_c(t)}{R} = \frac{22Ve^{-t/263.2ms}}{4.7k\Omega}$

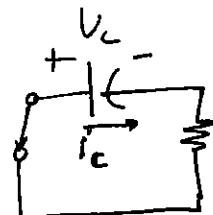
Post. 1
$$i_c(t) = 4.68mA e^{-t/263.2ms} \quad 0 < t \leq 1s$$

10-25a

$$V_C(1s) = 22V \left(1 - e^{-\frac{t}{263.2s}}\right)$$

$$= 21.51V$$

$$\begin{aligned} i_c(1s) &= -\frac{V_C(t=1s)}{R} \\ &= -\frac{21.51}{4.7k\Omega} \\ &= -4.58mA \end{aligned}$$



d) $V_C(t) = V_f + (V_i - V_f) e^{-t/\tau}$

For this problem τ remains the same

$$V_f = 0$$

$V_i = 21.51V$ The voltage V_C the instant the switch was thrown to position 2.

$$V_C(t) = 21.51V e^{-\frac{(t-1)}{263.2s}}$$

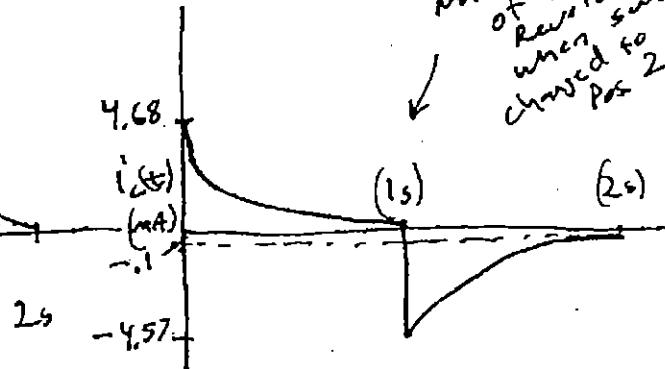
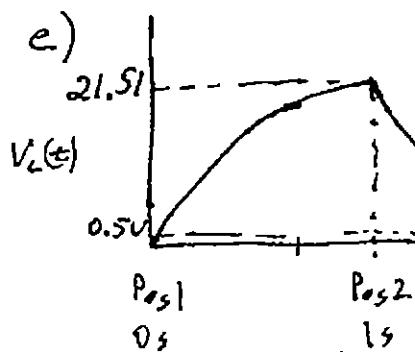
for $t \geq 1s$

KVL: $V(t) = -V_C(t)$

$$\Rightarrow i_c(t) = \frac{-V_C(t)}{R} = \frac{-21.51V e^{-\frac{(t-1)}{263.2s}}}{4.7k\Omega}$$

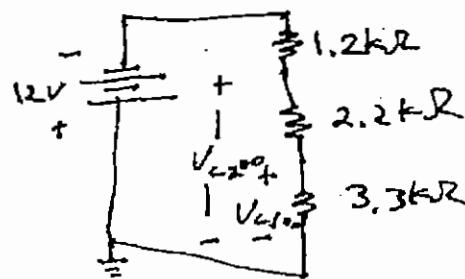
$$i_c(t) = -4.57mA e^{-\frac{(t-1)}{263.2s}}$$

for $t > 1s$



Note of Direction of current flow when switch changed pos 2.

55) Energy stored by a capacitor is given by $W_C = \frac{1}{2} CV^2$ therefore to answer the question we must know the voltage across each capacitor. Under steady state conditions capacitors act as an open circuit therefore we can simply find the voltages using Voltage Division.



$$V_{C100} = -12 \frac{3.3k\Omega}{6.7k\Omega}$$

$$= -5.91V$$

$$V_{C200} = -12 \left(\frac{5.5k\Omega}{6.7k\Omega} \right)$$

$$= -9.85V$$

$$W_{C100_F} = \frac{1}{2} (100 \times 10^{-6} F) (-5.91V)^2$$

$$= \boxed{1.75mJ}$$

$$W_{C200_{\text{F}}} = \frac{1}{2} (200 \times 10^{-6} F) (-9.85V)^2$$

$$= \boxed{9.7mJ}$$