

EE322 Fall 08 Homework Problem Set 37 (PS37)

Be sure to show your work.

1. Given the frequency response below, rewrite the equation for $H(j\omega)$ in the standard form for Bode analysis.

$$H(j\omega) = \frac{1000(j\omega + 1000)}{(j\omega + 10)(j\omega + 10,000)} = \frac{10^3 \cdot 10^3 \left(1 + \frac{j\omega}{10^3}\right)}{10 \left(1 + \frac{j\omega}{10}\right) \cdot 10^4 \left(1 + \frac{j\omega}{10^4}\right)}$$

$$= \frac{10 \left(1 + \frac{j\omega}{10^3}\right)}{\left(1 + \frac{j\omega}{10}\right) \left(1 + \frac{j\omega}{10^4}\right)}$$

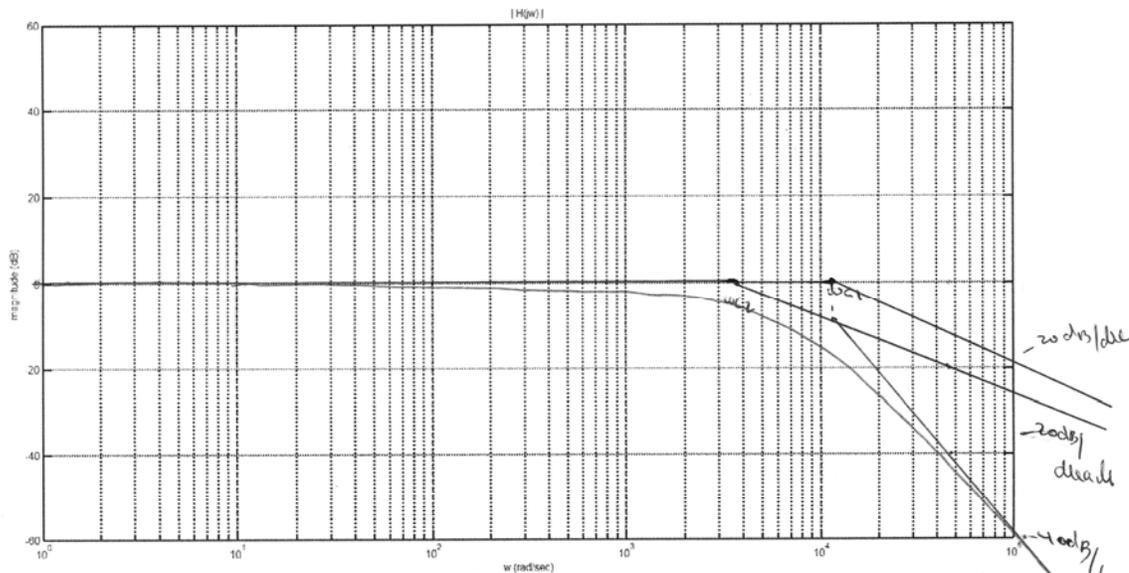
Indicate the following values from your answer to problem 3:

Gain term (constant) = 1

Zero(s) at $\omega =$ ∞

Pole(s) at $\omega =$ $2.61 \cdot 10^4$ rad/s & $0.38 \cdot 10^4$ rad/s

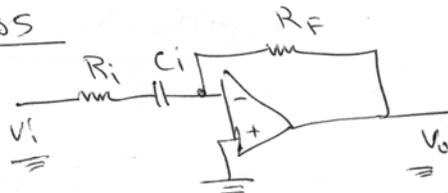
On the axis that follows, plot the asymptotic Bode magnitude of $H(j\omega)$. If the axes are hard to read, the x-axis runs from $\omega=10^0$ to $\omega=10^5$ rad/sec, and the y-axis runs from -60dB to +60dB.



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2. Text, problem 12-35. Use a constant gain term of +20dB and a cutoff frequency of 10 kHz, with a capacitor value of 0.01 μ F.
3. Text, problem 12-37c. Let all resistors = 100 Ω , and all capacitance = 1 μ F. Determine the equation for the frequency response, then plot the magnitude and phase in MATLAB. For the plotting, you can either:
- use the *abs/angle* functions with a semilogx plot for frequency, and convert magnitude to dB;
 - or use the *bode* function.

Pb 12-35



$$H(j\omega) = \frac{-R_f}{R_i + \frac{1}{j\omega C_i}}$$

$$f_c = \frac{1}{2\pi R_i C_i} = 10 \text{ kHz}$$

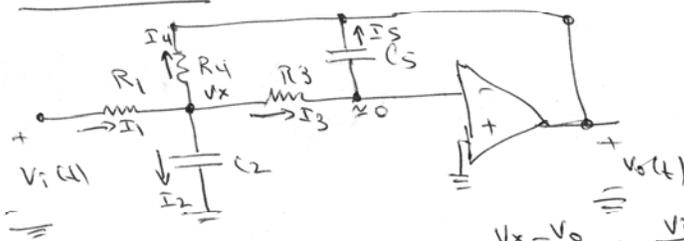
High frequency gain = $|H(\infty)| = R_f/R_i \Rightarrow 20 \log\left(\frac{R_f}{R_i}\right) = 20 \text{ dB}$

$$\Rightarrow \frac{R_f}{R_i} = 10 \Rightarrow \boxed{R_f = R_i \times 10}$$

2 equations, 2 unknowns $\Rightarrow R_i = \frac{1}{2\pi \cdot 10^4 \cdot 10^{-8}} = \frac{10^4}{2\pi} \approx 1.6 \text{ k}\Omega$

$$\boxed{R_f = 16 \text{ k}\Omega}$$

Pb 12.37c



① $I_1 = I_2 + I_3 + I_4$

② $I_3 = I_5$

$$\textcircled{1} \quad \frac{V_i - V_x}{R_1} = V_x(j\omega)C_2 + \frac{V_x - V_o}{R_4} + \frac{V_x}{R_3}$$

$$\frac{V_i}{R_1} = \frac{V_x}{R_1} + V_x(j\omega)C_2 + \frac{V_x}{R_4} - \frac{V_o}{R_4} + \frac{V_x}{R_3}$$

$$\boxed{V_i = V_x + V_x(j\omega)R_1C_2 + \frac{V_x R_1}{R_4} - \frac{V_o R_1}{R_4} + \frac{V_x R_1}{R_3}} \quad \textcircled{1}$$

$$\textcircled{2} \quad \frac{V_x}{R_3} = (0 - V_o)(j\omega)C_5 = -V_o(j\omega)C_5 \Rightarrow \boxed{V_x = -V_o(j\omega)R_3C_5}$$

Substitute ② in ①

$$V_i = -V_o \left[(j\omega) R_3 C_5 + (j\omega)^2 R_1 R_3 C_2 C_5 + (j\omega) \frac{R_1 R_3 C_5}{R_4} + \frac{R_1}{R_4} + (j\omega) \frac{R_1 R_3 C_5}{R_3} \right]$$

$$V_i = -\frac{V_o}{R_4} \left[(j\omega)^2 R_1 R_3 R_4 C_2 C_5 + (j\omega) C_5 (R_3 R_4 + R_1 R_3 + R_1 R_4) + R_1 \right]$$

$$H(j\omega) = \frac{V_o}{V_i} = - \frac{R_4}{(j\omega)^2 R_1 R_3 R_4 C_2 C_5 + (j\omega) C_5 (R_3 R_4 + R_1 R_3 + R_1 R_4) + R_1}$$

For $R_1 = R_2 = R_3 = R$ & $C_2 = C_5 = C$

$$H(j\omega) = - \frac{R}{(j\omega)^2 R^3 C^2 + (j\omega) C 3R^2 + R} = \frac{-1}{(j\omega)^2 RC^2 + 3RC(j\omega) + 1}$$

For $R = 100 \Omega$ and $C = 1 \mu F \Rightarrow RC = 10^{-4}$

$$H(j\omega) = \frac{-1}{(j\omega)^2 10^{-8} + 3 \cdot 10^{-4} (j\omega) + 1} = \frac{-1}{10^{-8} (j\omega + 2.61 \cdot 10^4) (j\omega + 0.38 \cdot 10^4)}$$

$$= \frac{-1}{\left(1 + \frac{j\omega}{2.61 \cdot 10^4}\right) \left(1 + \frac{j\omega}{0.38 \cdot 10^4}\right)}$$

$$20 \log |H(j\omega)| = \underbrace{20 \log |-1|}_0 - 10 \log \left(1 + \left(\frac{\omega}{\omega_{c1}}\right)^2\right) - 10 \log \left[1 + \left(\frac{\omega}{\omega_{c2}}\right)^2\right]$$

This is a low pass filter...when $\omega=0$, $H(j\omega)=1$ and when $\omega=\infty$, $|H(j\omega)| = 0$.