

Key

EE432 In-class exercise

Design an FIR LPF with the following specifications. Your final answer will be the equation for the impulse response of the filter, $h[n]$.

Pass band edge: 20 kHz

Stop band edge: 25 kHz

Stop band attenuation: 70 dB

Sample frequency: 100 kHz

① Transition width = $25 - 20 \text{ kHz} = 5 \text{ kHz}$

so $f_c = 20 \text{ kHz} + \frac{TW}{2} = 22.5 \text{ kHz}$

② $\Omega_c = \frac{2\pi f_c}{f_s} = \frac{2\pi \cdot 22.5 \text{ kHz}}{100 \text{ kHz}} = 0.45\pi$

$$h_1[n] = \frac{\sin(n\Omega_c)}{n\pi} = \frac{\sin(0.45\pi n)}{n\pi}$$

③ stop band Attenuation = 70 dB so use Blackman window

$$n = 5.98 \frac{f_s}{TW} = 5.98 \frac{100,000}{5000} = 119.6$$

use 119 = N

④ $h[n] = h_1[n] w[n]$

$$= \frac{\sin(0.45\pi n)}{n\pi} \left(0.42 + 0.5 \cos\left(\frac{2\pi n}{118}\right) + 0.08 \cos\left(\frac{4\pi n}{118}\right) \right)$$

$$\text{for } -\frac{(119-1)}{2} \leq n \leq \frac{119-1}{2}$$

$$-59 \leq n \leq 59$$

⑤ now shift $h[n]$ right by $\frac{N-1}{2} = 59$ values

$$h_{\text{LPF}}[n] = h[n-59]$$