

Name: \_\_\_\_\_

**EE451      Problem Set 1  
(Due 8/27/07)**

These problems are based on Anderson, Chapter 1. Please complete the problems in pencil on engineering paper and attach them by staple to this cover sheet.

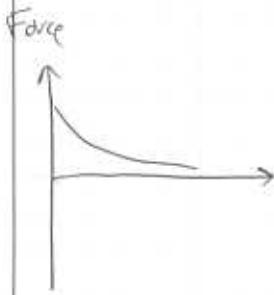
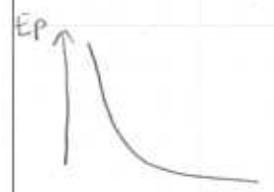
Review Questions: 1, 4, 5, 6, 7, 12

Problems 1.4, 1.8 parts a and b only, 1.14, 1.15, 1.19, 1.20, 1.21

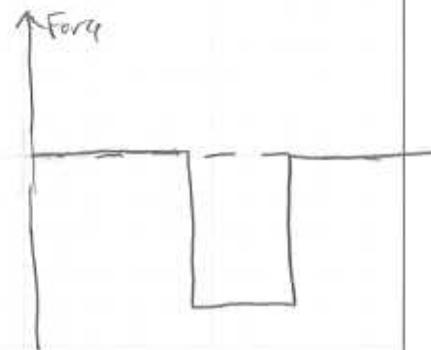
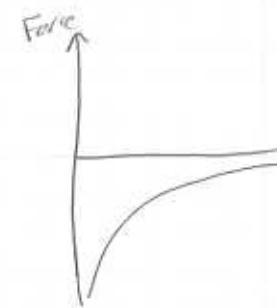
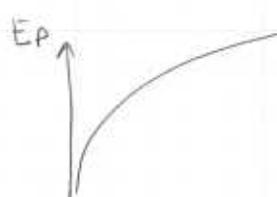
## Review

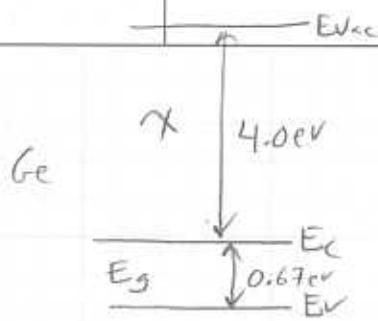
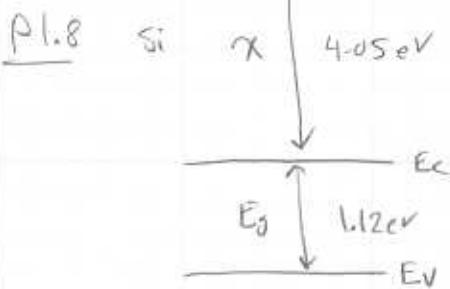
- 1  $1\text{eV} = 1.602 \times 10^{-19} \text{J}$  it is energy gained by an electron accelerated through a potential difference of 1 volt
- 4 each atom in the solid contributes energy states. These states can not be exactly the same - so they instead form a band of closely spaced states
- 5 Band gap of insulator is greater than band gap of semiconductor
- 6 Metals do not have full valence shells + do not completely bond - The valence electrons are free to move - There is no energy gap.
- 7 Thermal energy [phonons] increases with temp. This causes more electrons to be pushed into conduction band increasing conductivity
- 12 When a photon transfers its energy to an electron, the electron's energy increases by an amount equal to photon energy. The photon is annihilated - it ceases to exist.

## Problems 1.4



$$\underline{F = -\nabla EP}$$





P1.11  $10^6$  electrons/cm<sup>3</sup> in the conduction band

- There must be an equal number [density] of holes in the valence band - That is where the electrons had to come from
- Constant recombination of electron-hole pairs is offset by constant generation of electron-hole pairs.

P1.14 Wavelength

a)  $e^-$  with 1eV of KE  $E_{KE} = \frac{1}{2}mv^2 = \frac{(mv)^2}{2m} = \frac{p^2}{2m}$

$$p = \sqrt{2m E_K} = \sqrt{(2)(1.10 \times 10^{-31} \text{ kg})(1 \text{ eV})(1.602 \times 10^{-19} \text{ J/eV})}$$

$$\text{units } \left[ \text{kg} \text{ kg} \frac{\text{m}^2}{\text{s}^2} \right]^{1/2} = \text{kg} \frac{\text{m}}{\text{s}}$$

$$= 5.40 \times 10^{-25} \frac{\text{kg m}}{\text{s}}$$

$$\lambda = \frac{h}{p} = \frac{6.626 \times 10^{-34} \text{ J-s}}{5.40 \times 10^{-25} \frac{\text{kg m}}{\text{s}}} = 1.23 \times 10^{-9} \text{ m}$$

$$= 1.23 \text{ nm}$$

b)  $e^- E_K = 10 \text{ keV}$   $p \propto \sqrt{E_K}$  so  $p = \sqrt{10,000} 5.40 \times 10^{-25} \frac{\text{kg m}}{\text{s}}$  ↑ from above

$$\lambda = \frac{h}{p} = \frac{1.73 \text{ nm}}{\sqrt{10,000}} 0.0173 \text{ nm}$$

c)  $\lambda = \frac{h}{p} = \frac{h}{mv} = \frac{6.626 \times 10^{-34} \text{ J-s}}{(1 \times 10^9 \text{ kg})(1 \times 10^3 \text{ m/s})} = 6.626 \times 10^{-22} \text{ m}$

$$m_e \text{ mass} = 200 \text{ lb} = 90.9 \text{ kg}$$

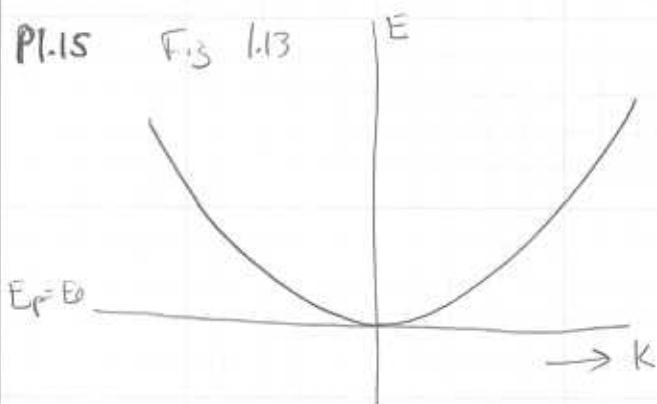
$$v = \left(4 \frac{\text{miles}}{\text{hr}}\right) \left(\frac{5280 \text{ ft}}{\text{mile}}\right) \left(\frac{0.3048 \text{ m}}{\text{ft}}\right) \left(\frac{1 \text{ hr}}{3600 \text{ s}}\right) = 1.79 \frac{\text{m}}{\text{s}}$$

$$\lambda = \frac{h}{p} = \frac{6.626 \times 10^{-34} \text{ J-s}}{(90.9 \text{ kg})(1.79 \frac{\text{m}}{\text{s}})} = 4.07 \times 10^{-36} \text{ m}$$

b The size of atoms is on the order of angstroms  $\text{A}^\circ = 10^{-10} \text{ m}$

Wavelengths of large bodies is much smaller than atomic size -

Pl.15 Fig 1.13



at bottom of parabola  $K=0$

$$\text{Thus } \lambda = \frac{2\pi}{K} \rightarrow \infty$$

Wavelength is infinite

$$E_K = \frac{p^2}{2m} \quad p = \frac{h}{\lambda} = \phi$$

so  $E$  is  $\phi$

$$\text{Pl.19 a) } E_2 \rightarrow E_1 \quad \Delta E = E_2 - E_1 = (E_{\text{vac}} - 3.4 \text{ eV}) - (E_{\text{vac}} - 13.6 \text{ eV}) \\ = 10.2 \text{ eV}$$

$$\Delta E = h\nu = \frac{hc}{\lambda} \quad \lambda = \frac{hc}{\Delta E} = \frac{(6.626 \times 10^{-34} \text{ J-s})(3 \times 10^8 \text{ m})}{(10.2 \text{ eV} \times 1.602 \times 10^{-19} \frac{\text{J}}{\text{eV}})} \\ = 122 \text{ nm}$$

$$\text{b) } E_4 \rightarrow E_3 \quad \Delta E = (E_{\text{vac}} - 0.85 \text{ eV}) - (E_{\text{vac}} - 1.51 \text{ eV}) = 0.66 \text{ eV}$$

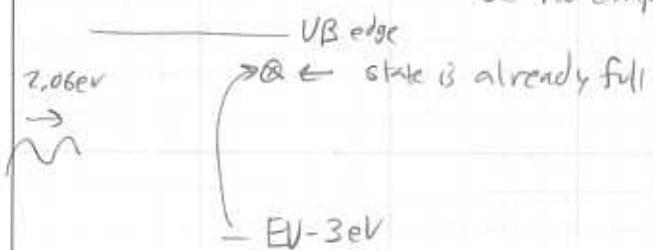
$$\lambda = \frac{hc}{\Delta E} = 1.9 \mu\text{m}$$

P1.20 a) Since  $E_2 \rightarrow E_1$  emits light with  $\lambda = 122$ , the same wavelength light will be absorbed by hydrogen

b) Light with  $\lambda = 430\text{ nm}$  has  $E = \frac{hc}{\lambda} = 2.88\text{ eV}$

will not be absorbed by Hydrogen since this energy does not correspond with any transition between states.

P1.21 a) an electron deep in conduction band [greater than 2.06eV below] can not absorb a photon with  $E = 2.06\text{ eV}$ . This is because the valence band is nearly completely full - There would be no empty state for the electron to move into



b) a photon is unlikely to be absorbed by an electron in the conduction band because the conduction band is very nearly empty -