

# Circuits Reference Card

## Physical Quantities

Quantity	Symbol	Units	Equivalents
Charge	$q$	coulomb	C
Current	$i = \frac{dq}{dt}$	ampere	$A = \frac{C}{s}$
Voltage	$v = \frac{dw}{dq}$	volt	$V = \frac{J}{C}$
Power	$p = \frac{dw}{dt}$ $= \frac{dw}{dq} \cdot \frac{dq}{dt}$ $= v \cdot i$	watt	$W = \frac{J}{s} = V \cdot A$
Resistance	$R = \frac{v}{i}$	ohm	$\Omega = \frac{V}{A} = \frac{W}{A^2} = \frac{V^2}{W}$

## Conservation Laws Material Properties

KVL (loop)  $\sum_k V_k = 0$       Resistance  $R = \frac{\rho \cdot l}{A}$

KCL (node)  $\sum_k I_k = 0$

## Useful Shortcuts

Series resistance

$$R_{\text{series}} = \sum_k R_k$$

Parallel resistance

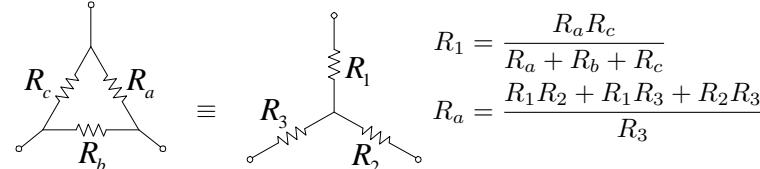
$$R_{\text{parallel}} = \frac{1}{\sum_k \frac{1}{R_k}}$$

Voltage divider (series)

$$v_{R_k} = \left( \frac{R_k}{R_{\text{series}}} \right) V_s$$

Current divider (node)

$$I_{R_k} = \left( \frac{R_{\text{parallel}}}{R_k} \right) I_s$$



## Nodal Voltage Analysis

- Choose a ground node (0 V) and label all other nodes.
  - Write current equations at labeled nodes using KCL.
  - Replace resistor currents using Ohm's law.
  - Replace resistor voltages using nodal voltages.
  - Solve the system of linear equations.
- Supernodes: voltage sources & elements in parallel with them.

## Mesh Analysis

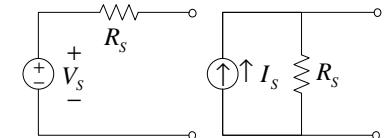
- Assign mesh currents  $i_k$  to each mesh loop.
  - Write voltage equations for each mesh using KVL.
  - Replace resistor voltages using Ohm's law.
  - Replace resistor currents with mesh currents
  - Solve the system of linear equations.
- Supermesh: exclude any current source & elements in series with it if they are shared by two meshes.

## Superposition

- Consider one *independent* source at a time. Kill all the others:
  - replace voltage sources with a short.
  - replace current sources with an open.
- Analyze the circuit with the single source and repeat.
- Sum the results.

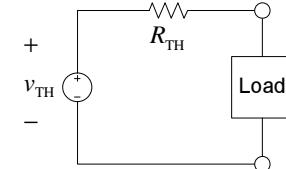
## Source Transformation

These two circuits behave identically if we choose  $V_S = I_S R_S$ .



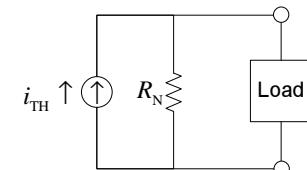
## Thévenin's Theorem

- Replace the load with an open.
- Find  $v_{TH} = v_{\text{open circuit}}$ .
- Kill the independent sources.
- Find  $R_{TH} = \frac{v_{TEST}}{i_{TEST}}$ .
- Restore the load.



## Norton's Theorem

- Replace the load with a short.
- Find  $v_N = v_{\text{short circuit}}$ .
- Kill the independent sources.
- Open circuit and find  $R_N = R_{TH}$ .
- Restore the load.



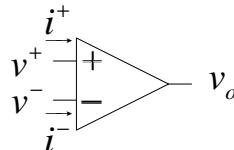
## Maximum Power Transfer

Choose  $R_L = R_{\text{TH}}$ .

$$P_{R_L} = \frac{V_{\text{TH}}^2}{4R_{\text{TH}}}$$

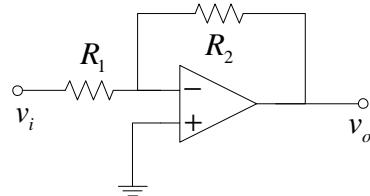
## Ideal Op Amp

- $v_o = A(v^+ - v^-)$
- $i^+ = i^- = 0$
- $R_{\text{in}} = \infty$
- $R_{\text{out}} = 0$
- $A = \infty$
- With negative feedback,  $v^+ \approx v^-$



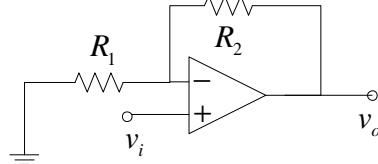
## Inverting Op Amp

$$v_o = -\frac{R_2}{R_1}v_i$$



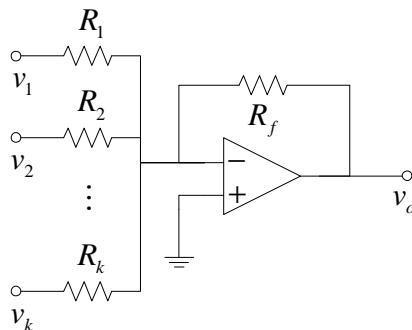
## Non-Inverting Op Amp

$$v_o = \left(1 + \frac{R_2}{R_1}\right)v_i$$



## Summing Op Amp

$$v_o = -R_f \sum_{i=0}^k \frac{v_i}{R_i}$$



## Capacitors and Inductors

**Quantity**    **Symbol**    **Units**    **Equivalents**

$$\text{Capacitance} \quad C = \epsilon \frac{A}{d} \quad \text{farad} \quad F = \frac{C}{V} = S \cdot s = \frac{s}{\Omega} = \frac{J}{V^2}$$

$$\text{Inductance} \quad L = \frac{N^2 \mu A}{l} \quad \text{henry} \quad H = \Omega \cdot s = \frac{J}{A^2}$$

$$q = Cv \quad i = C \frac{dv}{dt} \quad w_C = \frac{1}{2} Cv^2 \quad C_{\text{series}} = \frac{1}{\sum_i \frac{1}{C_i}} \quad C_{\text{parallel}} = \sum_i C_i$$

$$v = L \frac{di}{dt} \quad w_L = \frac{1}{2} Li^2 \quad L_{\text{series}} = \sum_i L_i \quad L_{\text{parallel}} = \frac{1}{\sum_i \frac{1}{L_i}}$$

$$\begin{array}{ll} \text{Voltage Divider} & v_{C_k} = \frac{C_{\text{series}}}{C_k} v_S \\ & v_{L_k} = \frac{L_k}{L_{\text{series}}} v_S \end{array} \quad \begin{array}{ll} \text{Current Divider} & i_{C_k} = \frac{C_k}{C_{\text{parallel}}} i_S \\ & i_{L_k} = \frac{L_{\text{parallel}}}{L_k} i_S \end{array}$$

## First-Order Circuits

$$v_C(t) = V_{C_F} + (V_{C_I} - V_{C_F}) e^{-(t-t_0)/\tau} \quad \tau = RC \quad V_{C_F} = v$$

$$i_L(t) = I_{L_F} + (I_{L_I} - I_{L_F}) e^{-(t-t_0)/\tau} \quad \tau = \frac{L}{R} \quad I_{L_F} = i$$

