

Assignment 30

Digital Logic

Name: Master Oct 28, 2002
 Section: 3311

- Use a Karnaugh map to generate minimal logic for a function F which will be true (1) if its 4-bit input is in the range 7 to 11 (inclusive) or if it is evenly divisible by 4.
- Manipulate the result so that it is implemented using 2-input NAND gates only. Draw a schematic for the resultant equation.

| | A | B | C | D | F |
|----|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 |
| 2 | 0 | 0 | 1 | 0 | 0 |
| 3 | 0 | 0 | 1 | 1 | 1 |
| 4 | 0 | 1 | 0 | 0 | 1 |
| 5 | 0 | 1 | 0 | 1 | 0 |
| 6 | 0 | 1 | 1 | 0 | 0 |
| 7 | 0 | 1 | 1 | 1 | 1 |
| 8 | 1 | 0 | 0 | 0 | 1 |
| 9 | 1 | 0 | 0 | 1 | 0 |
| 10 | 1 | 0 | 1 | 0 | 1 |
| 11 | 1 | 0 | 1 | 1 | 1 |
| 12 | 1 | 1 | 0 | 0 | 0 |
| 13 | 1 | 1 | 0 | 1 | 0 |
| 14 | 1 | 1 | 1 | 0 | 0 |
| 15 | 1 | 1 | 1 | 1 | 0 |

| | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| AB | 00 | 01 | 11 | 10 |
| 00 | 1 | 0 | 0 | 0 |
| 01 | 1 | 0 | 1 | 0 |
| 11 | 1 | 0 | 0 | 0 |
| 10 | 1 | 1 | 1 | 1 |

$$\begin{aligned}
 F &= AB\bar{C}\bar{D} + \bar{A}BCD \\
 &= \overline{\overline{AB\bar{C}\bar{D}} + \overline{\bar{A}BCD}} \\
 &= \overline{\overline{AB}\bar{C}\bar{D} + \overline{\bar{A}BCD}} \\
 &= \overline{\overline{AB}\bar{C}\bar{D}} \cdot \overline{\overline{\bar{A}BCD}} \\
 &= \overline{\overline{AB}\bar{C}\bar{D}} \cdot \overline{\overline{\bar{A}BCD}}
 \end{aligned}$$

To get 2-input NAND-gates only:

- Replace \bar{x} by $\overline{x \cdot x}$.
- Replace $x + y$ by $\overline{\overline{x+y}} = \overline{\overline{x} \cdot \overline{y}}$
- Replace $x \cdot y$ by $\overline{\overline{x \cdot y}}$

