

Computer Organization and Sequential Counters

CLOSED BOOK, CLOSED NOTES, ONE 8 1/2" x 11" SHEET PERMITTED

Name: Solution

Section: 3311

Date: 19 November 2002

Do not overlook the questions on the back of this sheet.

1. Consider a synchronous counter for four variables A, B, C, and D. In a truth-table laid out in a standard counting sequence where the most significant bit is A and the least significant bit is D, we find the desired next state of variable B is {0, 1, 1, 0, 1, 0, 0, 1, 1, 1, x, x, x, x, x, x}.

(a) Using a Karnaugh map, find minimal logic functions to operate the J- and K-inputs of a JK-flip-flop for variable B.

A	B	C	D	Next B	J _B	K _B	T _B
0	0	0	0	0	0	x	0
0	0	0	1	1	1	x	1
0	0	1	0	1	1	x	1
0	0	1	1	0	0	x	0
0	1	0	0	1	x	0	0
0	1	0	1	0	x	1	1
0	1	1	0	0	x	0	0
0	1	1	1	1	x	0	0
1	0	0	0	x	x	x	x
1	0	0	1	x	x	x	x
1	0	1	0	x	x	x	x
1	0	1	1	x	x	x	x
1	1	0	0	x	x	x	x
1	1	0	1	x	x	x	x
1	1	1	0	x	x	x	x
1	1	1	1	x	x	x	x

J _B		CD			
		00	01	11	10
AB	00	0	1	0	1
	01	x	+	+	+
	11	x	+	+	+
	10	1	1	+	+

$J_B = A + \bar{C}D + C\bar{D}$

K _B		CD			
		00	01	11	10
AB	00	x	+	x	x
	01	0	1	0	1
	11	x	+	+	+
	10	x	+	+	+

$K_B = \bar{C}D + C\bar{D}$

(b) Do the same for the T-input of a toggle flip-flop for variable B.

See T_B column above

T _B		CD			
		00	01	11	10
AB	00	0	1	0	1
	01	0	1	0	1
	11	x	+	+	x
	10	1	1	x	x

$T_B = A + \bar{C}D + C\bar{D}$

2. Suppose we desire a computer to be able to address 27000 different memory locations.

(a) What is the minimum number n of address lines the computer must use?

$$\text{we want } 2^n \geq 27000$$

$$n \log 2 \geq \log 27000$$

$$n \geq \frac{\log 27000}{\log 2}$$

$$\approx 14.7$$

$$\approx 15$$

We need at least 15 address lines.

(b) How many memory locations could be addressed in this system, beyond the 27000 required?

We can address $2^{15} = 32,768$ locations.

this is more than we need by

$$32,768 - 27,000 = 5,768$$