

Tugboat Swarms for Distributed Manipulation

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Swarm Manipulation

Army Ants: no communication, limited visual sense.

Humans: communicate only qualitative information during manipulation.

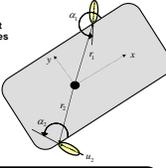



Can one design a distributed manipulation algorithm that requires **no communication** between swarm members?
To what extent does communication improve performance?

Force Control: Adaptive Approach

Dynamics: $M(\psi)\dot{\psi} + D\psi = BU$ ← Tug thrust magnitudes

Tug configuration matrix **UNKNOWN!** $B = \begin{bmatrix} \cos(\alpha_1) & \cos(\alpha_2) & \dots \\ \sin(\alpha_1) & \sin(\alpha_2) & \dots \\ r_1 \sin(\alpha_1 - \theta) & r_2 \sin(\alpha_2 - \theta) & \dots \end{bmatrix}$



Control: $U = [R(\psi)M^{-1}\hat{B}]^{-1} [\hat{P}_t + \alpha\dot{e} + K_r r + \psi \times \dot{P} + R(\psi)M^{-1}DR^T \hat{P}]$

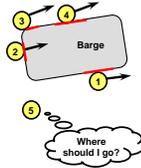
Adaptive update law estimates magnitudes of entries

Grasp Planning: Quality Function

Select **new** contact location to... ..apply largest wrench using smallest forces

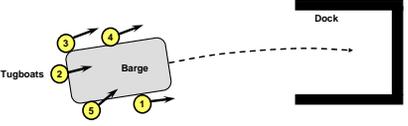
$$Q^* = \max_{B_N} \min_{w \in W} \max_{u \in U} \frac{\|w\|}{\|u\|}$$

Plan for worst case wrench direction **AND** Worst case locations of other tugs!



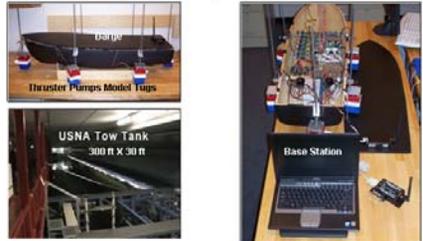
Where should I go?

Tugboat Mission



- Assume tugs "tie-up" to barge, actuator limits
- Non-trivial hydro-dynamics
- Distributed decision making
- Can use wireless messages to coordinate

Force Control: Experimental Set-up



Grasp Planning: Geometry

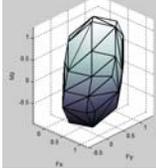
Set of possible wrenches under $L-\infty$ norm is a polyhedral in R^3 (a Zonotope)

Want to max/min distance from origin to closest facet (weakest direction)

$$\max_{B_N} \min_{B_i, \dots, B_{i-1}, B_{i+1}, \dots, B_N} \left(\min_{(j,k) \in \{1, \dots, P\}} \text{dist}(F_{jk}) \right)$$

Concave? $\text{dist}(F_{jk}) = \left(\sum_{i=1}^n \max \left[0, \frac{(B_i \times B_j) \cdot B_k}{\|B_i \times B_j\|} \right] \right)^2$

No. Determine which wrenches are active. But may be done a priori in certain cases. Yes. Second-order Cone. Easy to solve.



Related work

Swarms, Flock, Formations:

- Distributed control
- Kinematics objective

Cooperative Manipulation:

- Centralized /Static control
- Dynamic objective

Closely Related Works:

- Caging

Desai, Kumar, Fierro, Blahop, Tanner, Pappas, Jadbabaie, Passino, Olfes, Saber, Murray

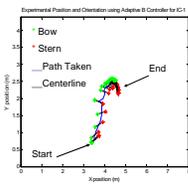
Zhaidong, Kumar, Ponce, et al.

Sugar, Brock, Khatib, Li, Lentz, Canny, etc

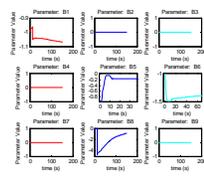


Force Control: Results

Experimental Position and Orientation using Adaptive B Controller for C1

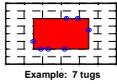


Converges to desired pose with small steady state error



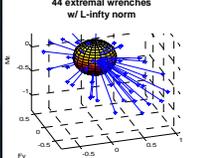
Unknown tug locations in B matrix are adjusted online

Grasp Planning: Results

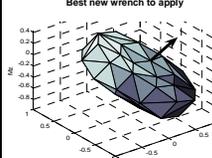


Example: 7 tugs

44 extremal wrenches w/ L-infinity norm



Best new wrench to apply



Sub-Problems and Approach

	Phase 1: Grasp Planning	Phase 2: Force control
Known	Own pose, barge pose, number of tugs, goal pose	
Uncertain	Exact attachment point of other tugs	
Find	Best attachment point	Best applied thrust
How?	Min-max grasp quality function	Adaptive control

Force Control: Conclusions

- Adaptive control provides a method to infer information about other swarm members **without communication**.
- Only a priori information is number of tugs and signs of moment arms.
- Experimental verification on 6 boats, needs to be generalized.

Grasp Planning: Conclusions

- Optimize a grasp quality function, max-min framework for uncertainty, $L-\infty$ norm unique geometry.
- Concave in certain cases. Scales well with swarm size. Makes computation easy.
- More investigation of concavity needed for general case.