SM121 Test I

14 SEP 2010

Name

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1. a) Find an equation for the line going through the point (2, 2) and perpendicular to the line 2y - x = 2.

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2. a) For the right triangle shown, which trigonometric function applied to θ gives a result of $\frac{\sqrt{5}}{2}$?



b) For the triangle in part a), find the angle θ (in radians) to two decimal places.

b) Graph and label both lines in part a) on the given set of axes.

3. Let f(x) be the second degree polynomial satisfying f(1) = f(2) = 0; f(0) = -2.

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a) Sketch the graph of y = f(x)on the axes to the right.

b) Find a formula for y = f(x).

c) Find the range for the function y = f(x).

4. The graph of a function y = f(x) is shown below.



On the same axes as y = f(x), a) Plot the graph of $y = f^{-1}(x)$ (inverse), and

(label your graphs.)

b) plot the graph of y = -f(x)+1.

5. If $f(x) = \sqrt{x}$ and g(x) = 2 - x,

a) find $(g \circ f)(x)$ and give its domain and range,

b) find $(f \circ g)(x)$ and give its domain and range.

6. Use your calculator and graph $y = x^3 + x$ and $y = \cos(2x)$ on the same axes below and determine any points of intersection accurate to 1 decimal place.



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7. a) If $\log_a(x) = 2$ and $\log_a(y) = 3$, find $\log_a(a^4x^3/y)$.

b) Solve for x to two decimal places if $9 = 4 + 5(e^{2x} - 3)$.

8. If we start with 10 grams of radio-active material, and it decreases by $\frac{1}{2}$ every 4 days (half-life),

a) How much material is left after 8 days?



c) Find a formula for the amount M as a function of t.

d) At what time will the material equal 0.1 grams?