

Name\_\_\_\_\_

Books and notes are closed. Calculators are open, loaded with any information you please; calculators may not be lent or borrowed. Intermediate work must be shown.

Hand this question sheet in with your answer booklets, and make sure each booklet has your name.

1 Solve the inequality  $|x - 13| < 100$ .

2a Define the convergence of the sequence  $a_n$  to the limit  $L$ .

2b Prove that the sequence  $a_n = \frac{1}{\sqrt{n}}$  converges and find the limit.

2c Use the squeeze theorem (sandwich theorem) to find the limit of  $\{\frac{\cos n}{\sqrt{n}}\}$ , justifying your answer.

3 Set up the integral to find the area in the first quadrant between the curves  $y = x^2$  and  $y = \sqrt{x}$ . Then solve.

4a Give the definition of “derivative” using limits. Use that definition to find the velocity if the position is  $\sqrt{1+t}$ . No quick Newton formula, please.

4b Take the derivative with respect to  $x$  of  $\cos(x \cos x)$ , using Newton’s formulas and methods.

5a If  $y^3 + x^5 + xy = 3$ , find an equation of the tangent to that curve at  $(1,1)$ .

5b If displacement is given by  $s(t) = 8 + \frac{1}{7} \sin(12\pi t)$ , where  $t$  is time, find velocity and acceleration.

6 Graph the curve  $y = 3x^2 - 12x + 5$  on  $[0,3]$ . Show and label the intervals where it is increasing, decreasing, concave upward, or

concave downward; show and label any inflection points. Find the absolute maximum and absolute minimum on  $[0,3]$ .

7 Show that the equation  $1 + 2x + x^3 + 4x^5 = 0$  has exactly one root.

8 The radius of a right circular cylinder is increasing at six inches per minute. The height is two feet. How fast is the volume increasing when the radius is three feet?

9 Get an approximation to  $\sqrt{10}$  using differentials (or, equivalently, using a linear approximation.)

10 Find the dimensions of a rectangle with area 500 square meters whose perimeter is as small as possible.

11a Evaluate  $\int_2^3 x^{-5} + 17x + \sqrt{x} dx$ .

11b Evaluate  $\int_1^4 \frac{\sin \sqrt{x}}{\sqrt{x}} dx$ .

11c Evaluate  $\int_0^{\pi/2} \frac{\sin x}{(1 + \cos x)^2} dx$ .

12 Find the point on the line  $y = x$  which is closest to the point  $(3,1)$ .

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